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Selecting and Fitting Expressive Growth Equations for Different Body Shapes of Fishes

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Abstract

Three relationships: age-length, age-weight, and length-weight in 31 fish species with 14 types of body shapes were fitted and selected through the computer following the principle of least squares sum. Sixty-three out of the 86 cases were fit to be expressed using the quadratic equation, $Y=a + bx + cx^2$, which accounted for 73.256% of the total number of cases. Checking computations and comparisons were made with the growth of silver carp *Hypophthalmichthys molitrix* that also served as an example.

Introduction

The study on age and growth is a basic content of fish biology. To be able to estimate fish resource dynamics and program fishery management in certain waters, it is equally important to find out the relationship between age and growth and express it in mathematical ways. To date, many of the scientific workers who have contributed a lot in this aspect (Qingjiang 1975; Chuanfuh et al. 1978; Shiqin and Yachu 1980; Zhonglin et al. 1981; Qiyong et al. 1981; Xuezu and Mingcheng 1983; Yuhao and Xiaopin 1984; Bangxi 1984; Bangxi et al 1986; Zhaohe 1987; Shushun et al. 1989; Sifa et al. 1990; Makang et al. 1990; Yongle et al. 1990; Guoying 1990; Dong and Jianlong 1990; Zhiling et al. 1990; Qigui and Xuefu 1992; Mingsheng 1993) employed the von Bertalanffy (1938, 1957) growth equation to express fish growth. Fabens (1965) reported the properties and fitting of von Bertalanffy growth curve. Allen (1966) performed a fitting study on the von Bertalanffy curve using the least squares sum method. Although a number of scholars proposed that in fitting the growth of fishes, it is better to use the quadratic 18

equation than the von Bertalanffy and logistic (Pearl and Reed 1920) equations, only a few utilized the quadratic equation due to its complicated computations (Kefei 1987; Changcheng 1990). Furthermore, some researchers believed that the characteristics of fish growth varied with fish species and their body shapes. Even if fishes were of the same shape or of the same species in different environments, their growth characteristics also differed a lot accordingly. Therefore, the appropriate growth expressions were not identical either (Yuanyu and Chuanlin 1981; Yuanyu and Jingrong 1983). In view of the facts presented, the study on fitting and selecting growth equations for different body shapes of fishes was made not only to meet the need of transferring fish biology data from qualitative description to quantitative analysis, but also to provide basis for fitting and selecting the best equation to be used in expressing the relationship between age and growth in fishes.

Materials and Methods

The main cultured fishes with different body shapes in China's freshwaters were chosen for the fitting study. Similarly shaped fishes were grouped into one shape pattern. Thirty-one species of commonly found fishes were grouped into 14 shape patterns in the light of geometric differences in the externals (Table 1). The specimen number of each fish is listed in table 1.

Eight equations most commonly used in biology to describe the growth of fishes were synthetically programmed in the computer (Program omitted here). Judged by the least squares sum, three groups of data, i.e. the data of age (Y) and body length (L), age and body weight (W), and body length and body weight of the 31 fishes with 14 body shapes were entered into the computer and formulated. According to the initial measured data, the units of body length of all the 31 fish species were in expressed centimeters. The units of body weight of common carp, black carp, yellow cheek carp and seasonal shad were in kilograms, while the other species were in grams. As to age, month was employed for icefish, and year for all the others. The eight equations used in the studies are listed in table 2.

Results

Three relationships (age-length, age-weight, and length-weight) describing the growth of fishes were fitted using the eight equations listed in table 2. Out of the 86 cases, 63 were well expressed using the quadratic equation (Table 1). Among these, age-length correlation accounted for 16 cases, agebody weight for 24 cases and length-weight for 23 cases, which constituted 73.256% of the total number of cases. Eight cases were suitable for logistic equation, among which, two cases were for age-length correlation, three were for age-weight and three were for length-weight, with a proportion of 9.302% of the total cases. Three cases with a proportion of 3.488% were fitted using the hyperbolic equation, while six cases were fitted using the power equation. Among these, age-length and length-weight correlations each accounted for the three cases respectively, with a proportion of 6.977% of the total cases. Six cases of age-length could be expressed using the logarithmic equation with a proportion of 6.977%. Linear equation, exponential equation and inverse equation were removed because they were not selected in the computations.

Discussion

In a biological study, logistic growth equation is the classic equation used to express fish growth. The shape of the equation is an S-curve. Theoretically it reflects various growth characteristics during different periods in the overall life cycle of fishes. Generally, the curve is divided into five growth stages: initial stage, accelerating stage, inflecting stage, decelerating stage and stagnating stage. These five stages may be expressed using related equations respectively. There is a growth inflection point during the inflecting stage. The asymptotic value C of the curve may be used as the maximum carrying capacity of the environment.

With reference to the stages Yanling et al (1981) gave a rather detailed description while studying the relationship between primary production and fish yield in waters. However, when the logistic equation was used to deal with the data, obtaining the parameters requires long life cycles of fishes and integrated age groups with enough samples, especially with a certain number of samples of the youngest and oldest age groups. Otherwise it is difficult to calculate the parameters of equation. This may cause errors between the calculated results and the actually measured values.

The von Bertalanffy growth equation was derived on the basis of fish energy metabolism, assuming that the body weight of fish is proportional to the body length's volume. The samples' conditions in applying this equation are the same as the logistic equation, and the characteristics of growth are not as objective as the latter. This can be seen from the difference in the figures of the first and last growth stages. Since the shape of the von Bertalanffy curve is an asymmetric "S" curve, it often results to some errors between the calculated and the actually measured values of samples from the youngest and the oldest age groups. The generation of these errors is known as the Rosa Lee Phenomenon (Richer 1975). Pitcher (1982) also gave a detailed discussion on the application of the von Bertalanffy growth equation.

It is worth demonstrating that both the quadratic equation and the von Bertalanffy growth equation are the same in reflecting growth characteristics and both required sample compositions. However, the former hardly shows the Rosa Lee phenomenon. Based on the actually measured data of 169 silver carps, checking computations and comparisons were performed between the two equations (Table 3). The result showed that the formulated values of quadratic equations were closer to the measured values than that of the von Bertalanffy equation.

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Table 1. Selecting and fitting on optimum expressive equations of growth for different body shapes of	fishes.

Body shape	Fish species	Specimen number	Relation- ship	Selected optimum expression						Express equation	Value of least residue quadratic sum	
				12	3	4 5	6	7	8		Sulli	
Silver	Silver	169	L- Y						•	$L=36.2199+3.4771Y+0.8571Y^2$	7.3982	
arp	carp		W-Y						•	$W = 2580.8730 - 1398.2460 Y + 536.4659 Y^2$	1.5534×10 ⁵	
haped			W-L						٠	$W=6.1998-0.2931L+4.4053\times 10^{-3}L^2$	0.2020	
	Bighead	30	L-Y						•	L=28.2856+6.0083 Y+0.7654 Y ²	35.3452	
	carp		W-Y <i>W-L</i>					•		$W=19.1495 \cdot (1+190.1369 \ e^{-0.06880L})^{-1}$	2.6085 1.1866	
			W-L					•			1.1800	
Grass	Black	38	L-Y	•						$L=7.0659+57.2512 \lg Y$	29.8305	
arp	carp		W-Y						•	$W=-5.0799+3.1806 Y+0.1392 Y^2$	1.3531	
shaped	Course	74	W-L L-Y			•				$W=3.2013\times10^{-5}L^{2.8330}$ L=25.3499+11.2053 Y-0.2089 Y ²	0.7603 55.6932	
	Grass carp	74	W-Y						•	$W = Y \cdot (1.1614 - 0.1105 \text{ Y})^{-1}$	1.8813	
	carp		W-L				•		•	$W=3.1247-0.1799L+3.3017\times10^{-3}L^2$	0.2870	
	Babel	166	L-Y							L=16.0344+13.21611gY	2.7365	
	chub	100	W-Y						•	$W = -9.0941 \times 10^{-2} + 0.1527Y + 6.5676 \times 10^{-3}Y^{2}$	8.1011×10 ⁻²	
			W-L						•	$W = 0.9819 - 9.3313 \times 10^{-2} L + 2.4302 \times 10^{-3} L^{2}$	0.512	
	Yellow-	229	L- Y				•			$L = Y \cdot (1.9112 \times 10^{-2} + 4.3503 \times 10^{-3} Y)^{-1}$	11.6876	
	cheek		W-Y						•	$W = -5.0297 + 5.0185Y + 0.2885Y^2$	8.9211	
	carp		W-L			•				$W=8.4953\times10^{-6}L^{3.1214}$	7.0186×10 ⁻⁴	
	Striped	167	L- Y						•	L=23.0101+10.1478 Y-0.6221 Y ²	0.9498	
	mullet		W-Y						•	$W = -0.1973 + 0.7016 Y + 1.6345 \times 10^{-3} Y^2$	5.6279×10 ⁻²	
			W-L						•	$W=1.5146-0.1082L+2.4222\times 10^{-3}L^2$	2.0434×10 ⁻²	
Common	Common	55	L- Y	•						L=22.4040+22.5369lgY	11.5180	
arp	carp		W-Y	-					•	$W = -0.1170 + 0.9159Y - 1.5358 \times 10^{-2}Y^{2}$	0.2323	
haped	P		W-L						•	$W=2.7028-0.1467L-2.9352\times 10^{-3}L^2$	9.1345×10 ⁻²	
	Crusian	48	L-Y				•			$L = Y \cdot (0.1695 + 2.0201 \times 10^{-2} Y)^{-1}$	6.7322	
	carp		W-Y						•	W=-32.1642+32.0625Y+2.8958Y ²	2.9691×10 ³	
	-		W-L						•	W=9.0079-6.5698L+0.9376L ²	6.3169×10^{2}	
	Nile	248	L-Y						•	L=16.6663-0.2005 Y+0.6623 Y ²	2.9044×10 ⁻²	
	tilapia		W-Y						٠	W=197.7035-21.1947Y+21.6457Y ²	14.3222	
			W-L							0.000731/ 1		
	Mud	214	L-Y					•		$L=65.6513 \cdot (1+4.7160e^{0.3067Y})^{-1}$	0.9019	
	carp		W-Y <i>W-L</i>						:	W=62.8043-96.2281Y+48.2631Y ² W=446.6630-60.8058L+2.1789L ²	3.8912×10 ³ 1.9139×10 ³	
			<i>11</i> <u>2</u>								110100.10	
Mandarin	Mandarin	73	L-Y			•				$L=14.2122 Y^{0.5610}$	0.1965	
ish baard	fish		W-Y						•	$W=2.3121\times10^{-2}+9.7658\times10^{-3}Y+4.0807\times10^{-3}Y$		
haped	T	40	W-L						•	$W=0.4812-5.9476\times10^{-2}L+2.1821\times10^{-3}L^{2}$ L=33.4503 $Y^{0.5514}$	3.2298×10 ⁻³	
	Japanese	49	L-Y W-Y			•			•	$W=1.9829-1.6495 Y+0.5588 Y^2$	4.3383 3.6238	
	sea perch		W-L						•	$W=1.3823^{-1.0433}I+0.3388I$ $W=8.8099-0.3950L+4.6898\times10^{-3}L^{2}$	5.1593	
		000	T N /							L 50 0571 (1 5 5000 -06541V)-1	10.0700	
Black	Black	632	L-Y					•		$L=56.3571 \cdot (1+5.5896e^{0.6541Y})^{-1}$ W=3632.8880 \cdot (1+140.0825e^{-1.0546Y})^{-1}	18.0708	
ream	bream		W-Y <i>W-L</i>					•	•	$W=3032.8880 \cdot (1+140.0825 e^{-1.00101})^{-1}$ $W=1103.4570 \cdot 107.0678L+2.7732L^{2}$	1.7596×10 ⁵ 2.0105×10 ⁵	
haped	Seasonal	348	L-Y						:	$L=34.9386+3.3571Y+3.3934\times10^{-2}Y^{2}$	11.6412	
	shad	340	W-Y							$W = -0.20 + 0.5975Y - 7.1446 \times 10^{-4}Y^{2}$	0.1536	
	Jinu		W-L						•	$W = -0.20 \pm 0.33751 + 7.1440 \times 10^{-1}$ $W = -7.6867 \pm 0.2422L + 8.2209 \times 10^{-4}L^2$	0.1818	
										_		
Puffer	Drab	575	L-Y						•	$L=74.3702+49.8422 Y \cdot 3.6089 Y^2$	36.4182	
haped	filefish		W-Y W-L						:	$W=-8.8604+46.0567 Y+0.4821 Y^{2}$ W=204.7198-2.9443L+1.3320×10 ⁻² L ²	3.2718×10 ² 32.7406	
			W-L						-	W-804.7100-2.0440L+1.0320A10 L	52.7400	
Redfin	Mongolian	201	L- Y	•						L=13.6235+13.8064lgY	6.5002	
ulter	culter		W-Y						•	W=2.3492×10 ⁻² +5.3163×10 ⁻² Y+1.0699×10	⁻² Y ² 4.1832×10 ⁻³	
haped			W-L						•	$W=0.4423-0.0445L+1.3734\times 10^{-3}L^2$	8.9981×10 ⁻³	
	Estuarine	765	L-Y						•	L=17.8799+1.8671 Y+0.4071 Y ²	27.9302	
	tapertail		W-Y						•	W=-21.80+28.5571Y+2.3571Y ²	3.9841×10 ³	
	anchovy	07	W-L						•	$W=178.0174-17.4588L+0.4847L^2$	4.3880×10 ²	
	Sharpbelly	67	L-Y W V						•	$L=2.3600+4.7071 Y-0.2928 Y^{2}$ W=89.3239 (1+28.5159e ^{-1.009 Y}) ⁻¹	4.6286×10 ⁻²	
			W-Y W-L					•	•	$W=89.3239 \cdot (1+28.5159e^{-1.0091})^{-1}$ $W=20.0797 \cdot 4.5075L + 0.4098L^2$	70.7559 50.2535	
											_	
mall-scale	Small-scale	197	L-Y						•	L=13.1600+7.9328 Y-0.6357 Y ²	1.2277×10 ⁻²	
ellow-fin	yellowfin		W-Y						•	$W=-0.0694+0.2301 Y-9.0177\times 10^{-3} Y^{2}$	0.3005	
haped	a	10.1	W-L						•	$W=0.2081-2.8575\times10^{-2}L+1.2640\times10^{-3}L^2$	1.7777×10 ⁻²	
	Spotted	484	L-Y	•						$L=3.4554+12.9372 \lg Y$	26.6938	
	steed		W-Y W-L						:	$W=-2.8111+22.3277 Y+3.1730 Y^2$ $W=26.7517-10.4916L+0.7485L^2$	82.1942 82.6107	
									-			
nake-head	Snakehead	52	L-Y W V						•	$L=21.8705+3.8349Y+1.1750Y^2$	4.5001×10 ⁻³	
haped			W-Y						•	W=590.8503-454.40 Y+228.40 Y ²	1.4045×10^{2}	
			W-L						٠	W=734.5490-55.5545L+1.5337L ²	3.0486×10 ³	

continued

Table 1 continued

Body shape	Fish species	Specimen number	Relation- ship	Selected optimum expression							ı	Express equation	Value of least residue quadratic	
				1	2	3	4	5	6	7	8		sum	
catfish	Long-snout	303	L- Y								•	L=9.1507+12.8380 Y+0.4571Y ²	11.7825	
shaped	catfish		W-Y								٠	$W = -0.5055 + 0.4731 Y + 4.1192 \times 10^{-2} Y^2$	0.1222	
			W-L								٠	W=0.0919-2.3760×10 ⁻² L+1.1155×10 ⁻³ L ²		
	Chinese	174	L-Y			٠						L=40.6131 Y ^{0.4867}	4.7164	
	sheatfish		W-Y								٠	W=-0.3185+0.8761 Y+0.1036 Y ²	0.2448	
			W-L			٠						$W = 8.9279 \times 10^{-2} L^{3.0161}$	0.1655	
	Burbot	219	L-Y		٠							L=29.8352+11.5953lgY	1.2028×10^{3}	
			W-Y								٠	$W=114.1006-61.0325 Y+49.1679 Y^2$	1.4121×10^{5}	
			W-L								•	$W = 245.5558 - 28.2608L + 0.9364L^2$	2.2108×10^{2}	
Rhinogobio	Rhinogobio	100	L- Y											
shaped	ventralis		W-Y											
-			W-L								٠	$W=20.6005-0.5178L+3.7769\times10^{-3}L^2$	1.4717×10 ⁻⁷	
	Pond	200	L-Y								٠	L=3.3200+4.8613 Y-0.1785 Y ²	0.4845	
	smelt		W-Y								٠	W=106.4197-77.2066 Y+20.7971 Y ²	1.8539×10^{4}	
			W-L							•		$W = 380.5085 \cdot (1 + 108.9006e^{-0.2492L})^{-1}$	25.2623	
Rice-field	Ricefield	210	L- Y								•	L=15.7469+9.7381 Y-0.2669 Y ²	10.8455	
Eel shaped			W-Y								•	W=49.1396-43.8254 Y+15.8713 Y ²	1.5047×10^{2}	
			W-L							•		W=1108.1130 (1+646.8310e ^{-8.7866×10-2L}) ⁻¹	2.7705×10^{3}	
	Japanese	31	L-Y											
	eel		W-Y											
			W-L								•	$W = 334.7548 - 24.5647L + 0.4661L^2$	2.1686×10^{3}	
cefish	Large	44	L- Y								•	$L=-22.3155+29.1017 Y-1.4445 Y^2$	1.4555×10 ²	
haped	ice-fish		W-Y											
			W-L											
loach	Loach	27	L- Y								•	$L=4.4500+3.9732 Y=0.1839 Y^2$	4.1785×10 ⁻²	
shaped			W-Y								•	$W=-6.6100+10.5475Y+0.5589Y^2$	20.9623	
			W-L									$W = -0.8389 - 1.0217L + 0.2106L^2$	30.2228	

Table 2. List of equations used in the study.

T	V - L-	1	
Linear equation	Y = a + bx	1	
Logarithmic equation	$Y = a + b \lg x$	2	
Exponential equation	$Y = ae^{bx}$	3	
Power equation	$Y = ax^b$	4	
Inverse equation	$Y = 1 \cdot (a + bx)^{-1}$	5	
Hyperbolic equation	$Y = x \cdot (a + bx)^{-1}$	6	
Logistic equation	$Y = c \cdot (1 + ae^{-bx})^{-1}$	7	
Quadratic equation	$Y = a + bx + cx^2$	8	

Table 3. Comparison of checking computation results by two equations for silver carp.

Age groups	Specimen no.		red body h (cm)		ured body ight (g)	Bertalanff	Quadratic equation		
		Range	Mean±SD	Range	Mean±SD	Body length ¹	Body weight ²	Body length ³	Body weight ⁴
1+	105	28.5-50.2	39.7±5.0	500-2800	1360.9±486.0	23.0788	254.9033	40.5541	1719.0929
2+	43	36.0-59.0	48.3±6.2	900-4450	2589.4±137.5	40.5972	1387.4632	46.6025	1930.2446
3+	15	43.0-64.8	54.4±5.6	2500-6250	3386.0±949.6	54.3693	3332.6976	54.3651	3214.3281
4+	3	50.0-70.0	61.2 ± 10.1	2500-6250	4683.3±1949.6	65.1964	5746.5162	63.8419	5571.3434
5+	3	74.2-79.0	75.9±2.7	7500-11500	9416.7±2005.2	73.7082	8303.8693	75.0329	9001.2905

 ^{1}L =105.0[1- $e^{0.2046(t+0.0316)}$]

 $^{2}W = 24005.0[1 - e^{-0.2046(t+0.0316)}]^{3}$

 $^{3}L=36.2199+3.4771Y+0.8571Y^{2}$

⁴W=2580.873-1398.246 Y+536.4659 Y²

It is further verified while analyzing the growth characteristics of the fishes with short life cycles and insufficient oldest and/or youngest age groups, that the application of quadratic equation is preferable. The results

were consistent with the views of Kefei (1987) and Changchen (1990). In the calculations of the 86 cases, 63 were well expressed using the quadratic equation and ranked first among the eight equations. Among the 29 cases of formulations of the relationship between body length and body weight, 23 were expressed using the quadratic equation, while power equation and logistic equation were each fitted in three cases but comparisons between the theoretical and actual values measured showed that power equation was the best.

The equation used in selecting the expressions of age and growth relationship based on the fishes' body shapes did not show the obvious selectivity in this paper. Only the values of parameters differred from each other when the same equation was utilized.

Conclusion

Two growth relationships, age-body length relationship and age-body weight relationship were suitably expressed using the quadratic equation, while length-weight relationship was appropriately described using the power function equation.

The various shapes of fishes did not show obvious selectivity to the eight equations used in this paper. Three equations, linear equation, exponential equation and inverse equation were not selected in the fitting calculations and were therefore removed.

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